

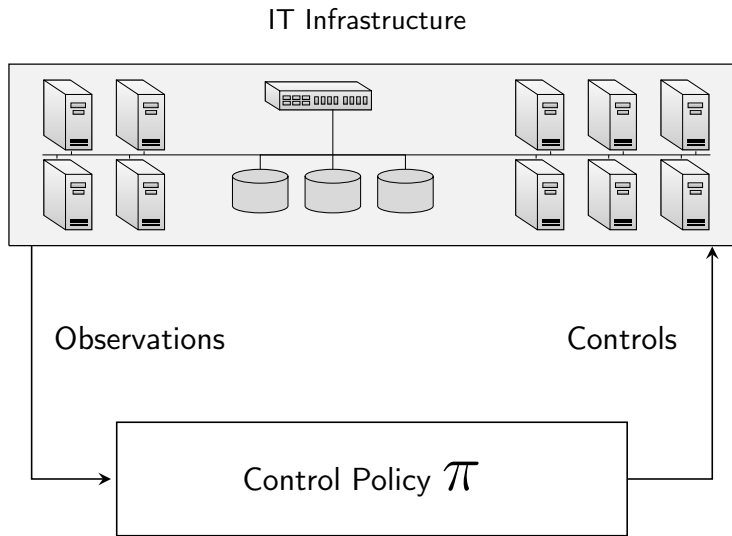
Self-Learning Systems for Cyber Security

NSE Seminar

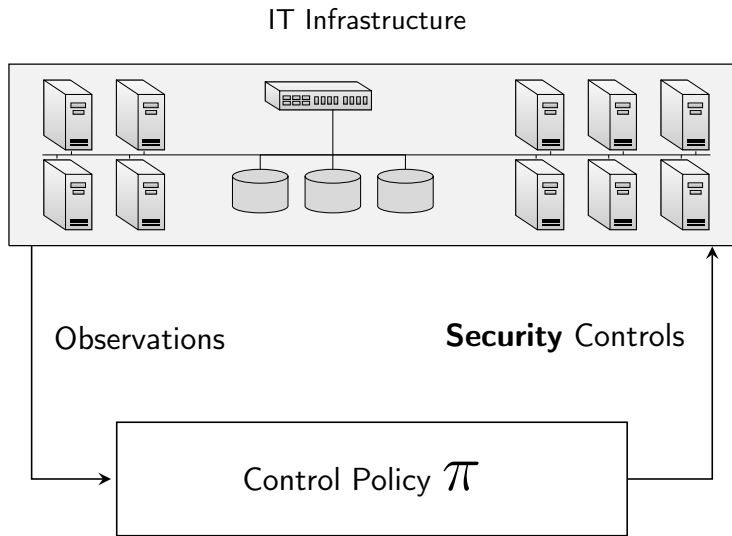
Kim Hammar & Rolf Stadler

December 4, 2020

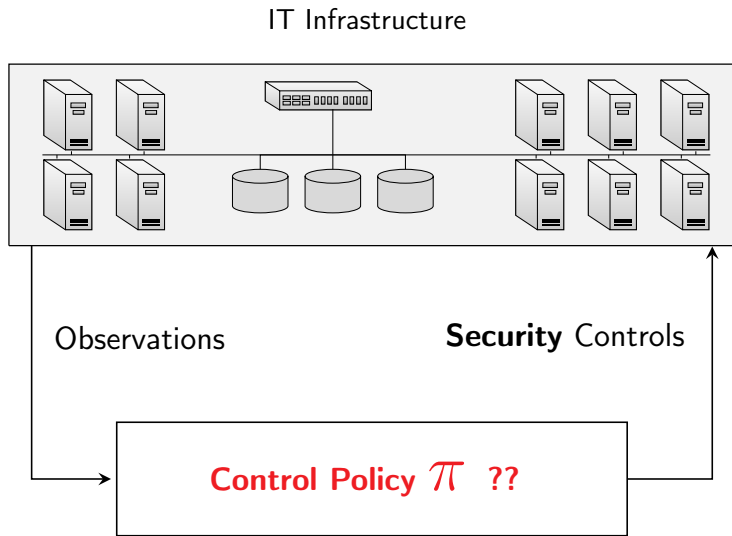
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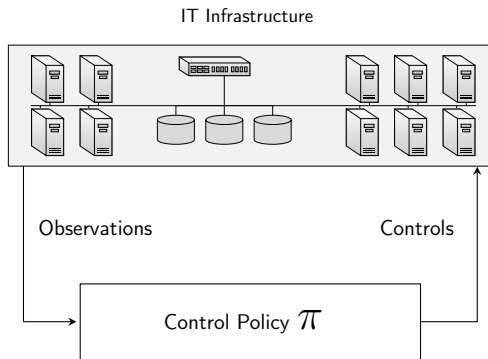
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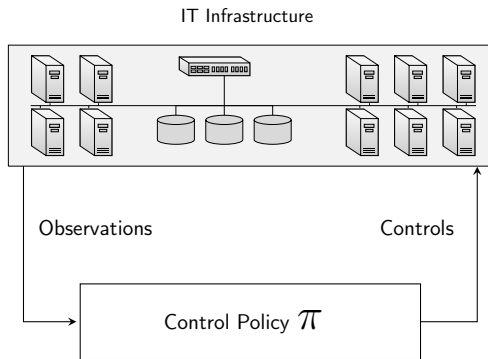
Self-Learning Systems for Cyber Security



▶ What are useful controls?

- ▶ Penetration tests
- ▶ Intrusion prevention strategies & Adaptive security policies
- ▶ Limiting virus spread
- ▶ ⋮

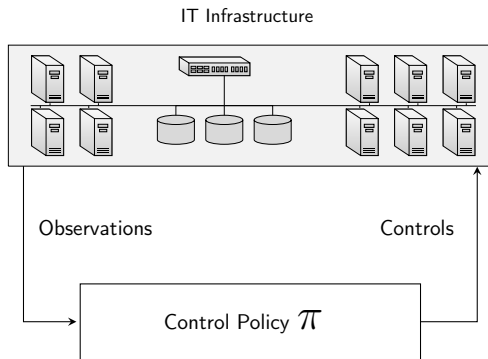
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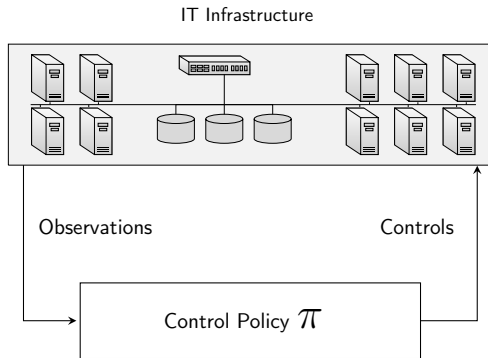
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Related Work

- ▶ **Model-Based Approaches:**
 - ▶ Optimal Control¹
 - ▶ Dynamic Programming²
 - ▶ Computational Game Theory³
- ▶ **Simulation-Based Approaches**
 - ▶ Evolutionary Methods⁴
 - ▶ Reinforcement Learning⁵

¹Jianguo Ren, Yonghong Xu, and Chunming Zhang. "Optimal Control of a Delay-Varying Computer Virus Propagation Model". In: *Discrete Dynamics in Nature and Society* 2013 (2013), p. 210291. ISSN: 1026-0226. DOI: 10.1155/2013/210291. URL: <https://doi.org/10.1155/2013/210291>.

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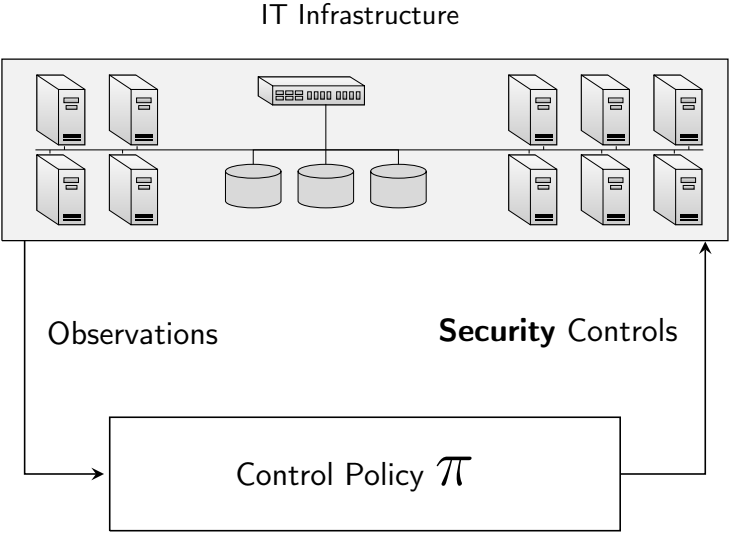
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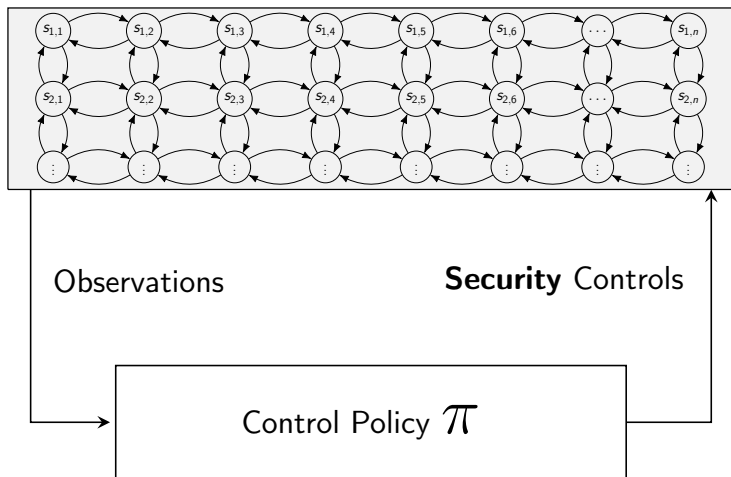
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Model-Based Control: DT Dynamical System Model



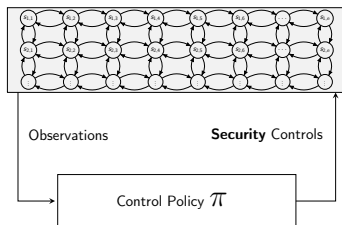
Model-Based Control: DT Dynamical System Model

$$\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{P}_{ss'}^a, \mathcal{R}_{ss'}^a, \gamma, \rho_0, T \rangle$$



Model-Based Control: DT Dynamical System Model

$$\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{P}_{ss'}^a, \mathcal{R}_{ss'}^a, \gamma, \rho_0, T \rangle$$



- ▶ \mathcal{M} = Markov Decision Process
- ▶ Problem reduces to solving Bellman's equations

$$u_t(h_t) = \sup_{a \in A_{s_t}} \left[r_t(s_t, a) + \sum_{j \in \mathcal{S}} p_t(j|s_t, a) \underbrace{u_{t+1}(h_t, a, j)}_{\text{-cost to go}} \right]$$

- ▶ Solution methods²¹: Backward induction, Dynamic programming (Value iteration, Policy iteration)

Limitations of the Model-Based Approach

Modeling Challenge

How to model complex systems and cyber attacks **accurately**?

Scalability Challenge

Models are often impractical due to scale of applications.

- ▶ e.g. assume MDP model of cyber range:

$$\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{P}_{ss'}^a, \mathcal{R}_{ss'}^a, \gamma, \rho_0, T \rangle$$

- ▶ Need to solve:

$$V^*(s) = \max_a \sum_{s' \in \mathcal{S}} \mathcal{P}_{ss'}^a [\mathcal{R}_{ss'}^a + \gamma V^*(s')]$$

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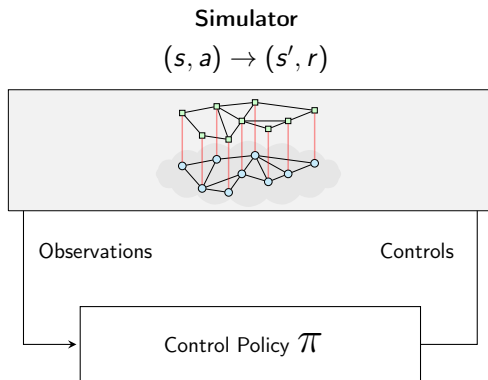
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- ▶ Need to solve (**curse of modeling**²²):

$$V^*(s) = \max_a \sum_{s' \in \mathcal{S}} \mathcal{P}_{ss'}^a [\mathcal{R}_{ss'}^a + \gamma V^*(s')]$$

$|\mathcal{S}| = 10^{170}$ (Atoms in the universe $\approx 10^{80}$)

Simulation-Based Approaches



- ▶ Rather than defining complete model
 $\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{P}_{ss'}^a, \mathcal{R}_{ss'}^a, \gamma, \rho_0, T \rangle \implies$ **define simulator that can be sampled from.**
- ▶ **Pros:** scalable, simple to implement, flexible
- ▶ **Cons:** (same as model-based) is it realistic??

Simulation-Based Example: Intrusion Prevention²³

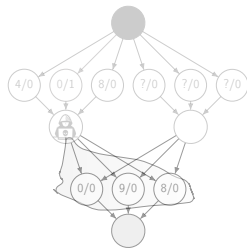
Question

Can effective security-strategies emerge from self-play RL?

- ▶ Model network as graph $\mathcal{G} = \langle \mathcal{N}, \mathcal{E} \rangle$
- ▶ Attack/defense attributes per node $S_k = \langle S_k^A, S_k^D \rangle$
- ▶ Simulate outcome of actions as function $f(s, a)$.
- ▶ Partially observed two-player Markov game

Results:

- ▶ Challenging learning task but possible
- ▶ ϵ -optimal strategies emerge using our proposed method
 - ▶ AR policy, opponent pool, PPO, function approximation
- ▶ Strategies are abstract, cannot easily be verified



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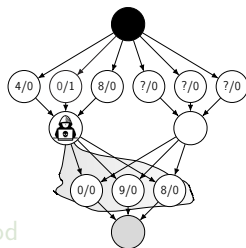
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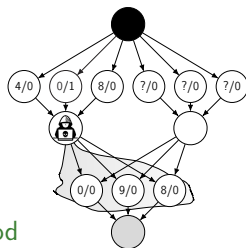
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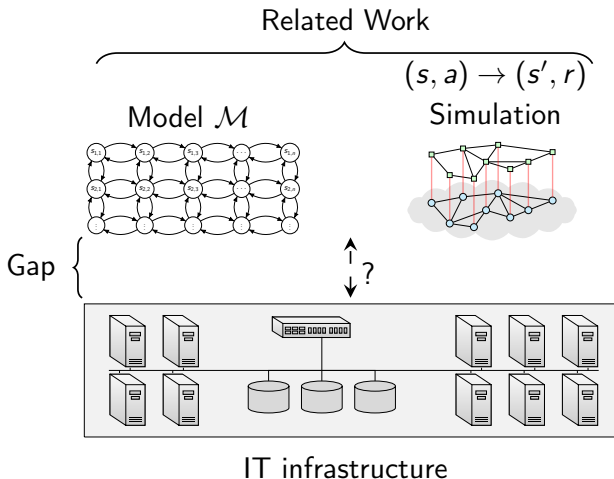
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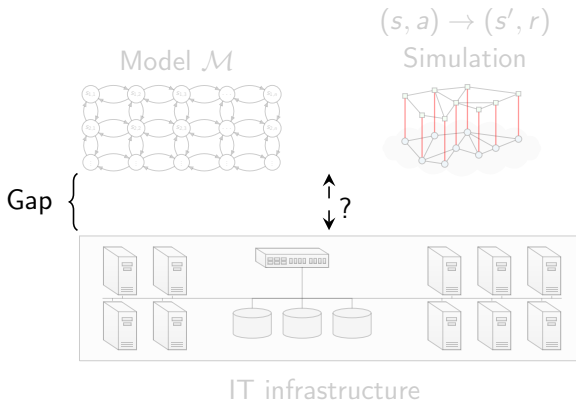
Research Questions

- ▶ Prior work focused on **simulation-based** and **model-based** approaches
 - ▶ *Assumed to be impractical to interact with real systems*



Research Questions

- ▶ How large is this gap? How can we bridge it?
- ▶ Take inspiration from early works studying this problem²⁶



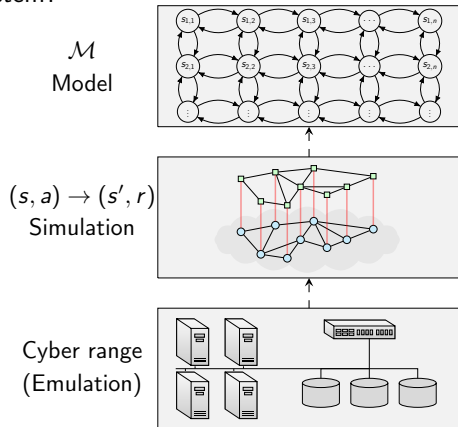
²⁶Gabriel Dulac-Arnold, Daniel J. Mankowitz, and Todd Hester. "Challenges of Real-World Reinforcement Learning". In: *CoRR* abs/1904.12901 (2019). arXiv: 1904.12901. URL: <http://arxiv.org/abs/1904.12901>, Hyrum S. Anderson et al. "Learning to Evade Static PE Machine Learning Malware Models via Reinforcement Learning". In: *CoRR* abs/1801.08917 (2018). arXiv: 1801.08917. URL: <http://arxiv.org/abs/1801.08917>, Piotr Gawlowicz and Anatolij Zubov. "ns3-gym: Extending OpenAI Gym for Networking Research". In: *CoRR* abs/1810.03943 (2018). arXiv: 1810.03943. URL: <http://arxiv.org/abs/1810.03943>.

Research Questions

Assumption

“Assumed to be impractical to interact with real systems”

- ▶ **Can we question this assumption?**
 - ▶ What is the right balance between model/simulation/real system?



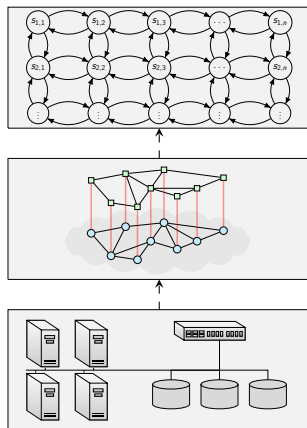
Our Approach

▶ Goals:

- ▶ Framework for learning control tasks in security
- ▶ Connect simulations & models with practical environment

▶ What is a good environment for evaluation?

- ▶ Cyber ranges
- ▶ Used to evaluate human security experts



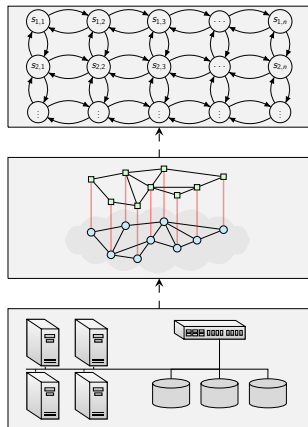
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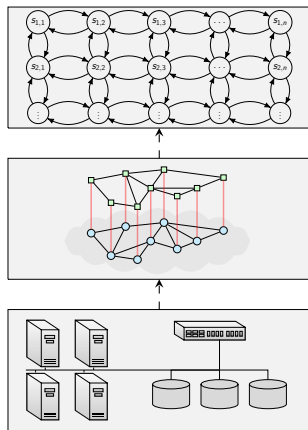
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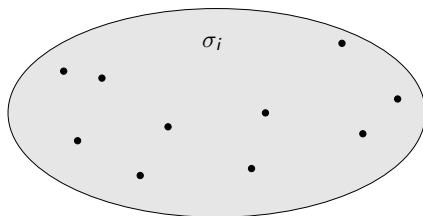


Idea

Need a **tool to generate cyber ranges** for different control tasks

Generation of Cyber Ranges for Control Tasks

$\Sigma = \langle \mathcal{C}, \mathcal{O}, \mathcal{S}, \mathcal{U}, \mathcal{T} \rangle$ Configuration Space

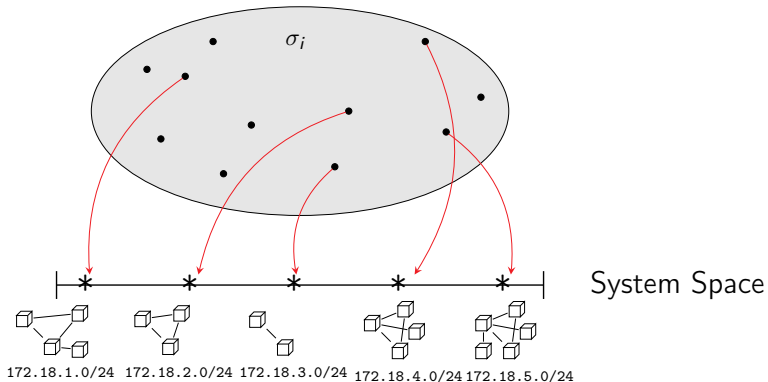


- ▶ The **configuration space**²⁷ defines the networks that can be generated.
- ▶ Controls \mathcal{C} (e.g. nmap, firewall configs, metasploit, etc.)
- ▶ Operating Systems \mathcal{O} (e.g. Kali, Ubuntu 20, etc.)
- ▶ Services \mathcal{S} (e.g. Kafka, MongoDB, NTP, etc.)
- ▶ User types \mathcal{U} (e.g. root, non-root, various groups)
- ▶ Topologies \mathcal{T} (implemented using firewall rules)

²⁷implemented with a set of docker images

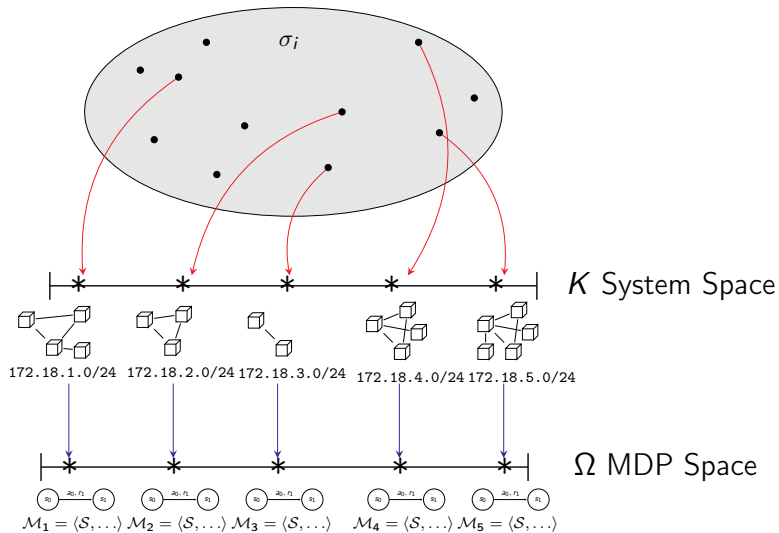
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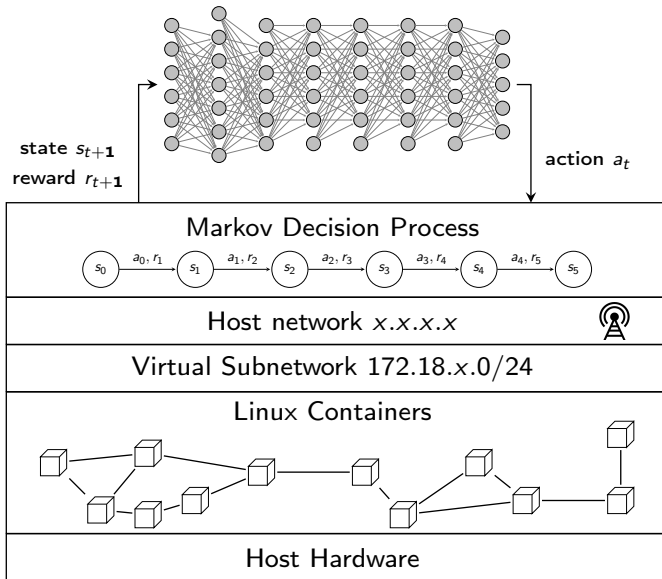


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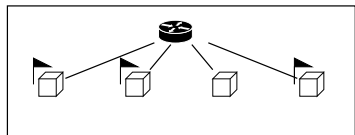
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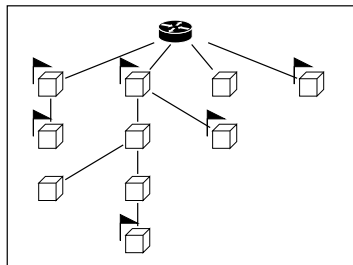
System Architecture



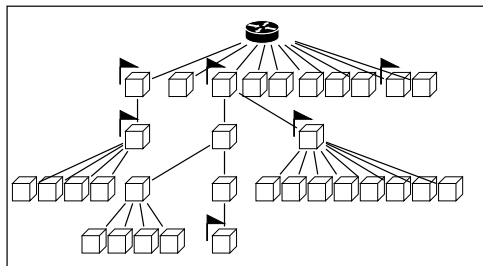
First Evaluation of Framework: **Learn** to Capture the Flag



Learning task v_1



Learning task v_2



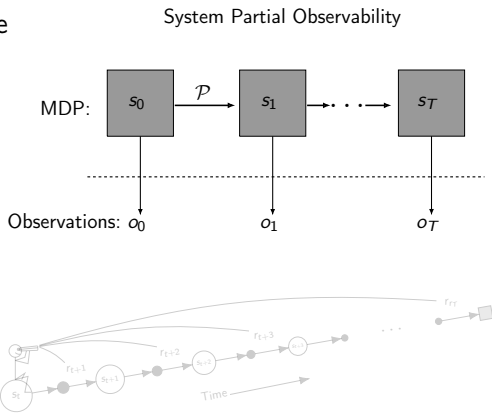
Learning task v_3

System Model (1/3)

- ▶ **Hidden Markov Model.** The agent estimates the state of the system based on a sequence of observations $o_1, o_2, \dots \in \mathcal{O}$

- ▶ **Infinite Discounted Time-Horizon.** Discrete time, decision epochs $T = \mathbb{N}_{\geq 0}$. Objective:

$$\max_{\pi} \mathbb{E} \left[\sum_{t=1}^{\infty} \lambda^{t-1} r(s_t, a_t) \right]$$

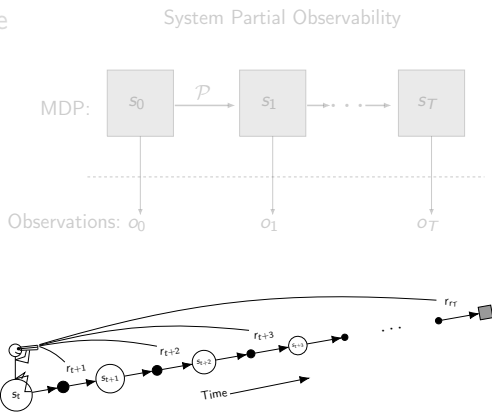


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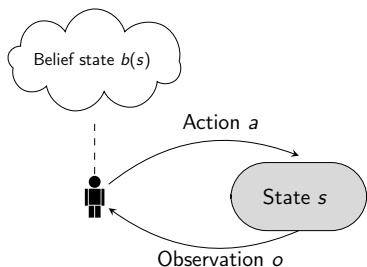
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System Model (2/3)



Let b_t be the **belief state** at time t

$$b_t(s) = \mathbb{P}[s_{t+1} = s | b_t], \quad s = \begin{bmatrix} p_{1,1} & p_{1,2} & \dots & sh_1 \\ \vdots & \vdots & \dots & \vdots \\ p_{N,1} & p_{N,2} & \dots & sh_N \end{bmatrix} \in \mathcal{S} \in \mathbb{R}^{N \times 34}$$

state estimated based on **basis functions** $\{\phi_1, \dots, \phi_{34}\}$ from observations o . e.g.

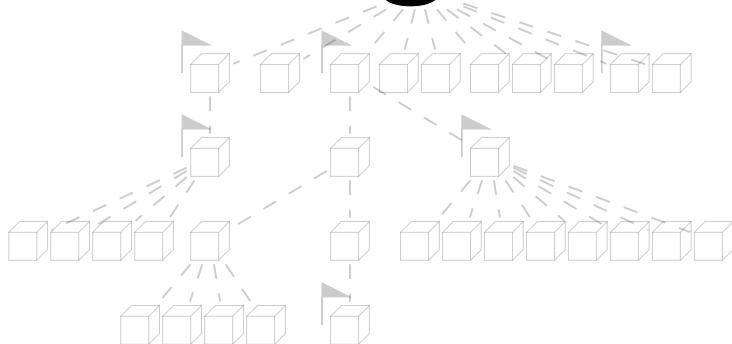
$$\phi_1(o) = \mathbb{1}_{\text{port 22 open}} \quad \phi_2(o) = \mathbb{1}_{\text{shell access}} \quad \dots \quad \phi_{34}(o) = \#\text{CVEs.}$$

System Model 2/3

$$b_t(s) = \begin{bmatrix} 0 & 0 & \dots & 0 \\ \vdots & \vdots & \dots & \vdots \\ 0 & 0 & \dots & 0 \end{bmatrix}$$



$$a = \arg \max_a \pi_\theta(a|s)$$



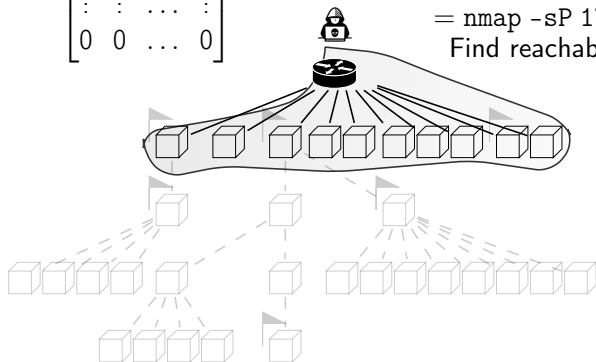
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= nmap -sP 172.18.3.0/24

Find reachable machines on network



System Model (2/3)

- ▶ Let $\mathcal{A} \triangleq \{\text{nmap}_i, \text{metasploit}_i, \text{nikto}_i, \dots\}$ be the **action space**. $\mathcal{A} \subset \mathcal{B}$ where \mathcal{B} is the set of commands of the Bash command-line.
- ▶ Let

$$r(s_{t+1} | a_t, s_t) = \begin{cases} 10 & \text{if } b_{t+1}^{\# \text{flags}} > b_t^{\# \text{flags}} \\ 0 & \text{if } b_{t+1} \neq b_t \\ -10 & \text{otherwise} \end{cases}$$

be the **reward function**, realizing the agent's objective to capture the flags in the system.

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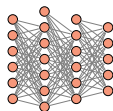
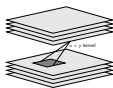
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System Model (3/3)

- ▶ As $|\mathcal{B}| \gg 10^{34}$, we rely on parameteric function approximation.
 - ▶ Consider parameterized policies π_θ
 - ▶ where $\theta \in \mathbb{R}^d \wedge d \ll 10^{34}$.
- ▶ We consider²⁸ the space of Non-Markovian History-Dependent Time-Homogeneous Mixed Policies $\pi : \mathcal{B} \mapsto \mathcal{A}$, $\pi \in \Pi^{HR}$.

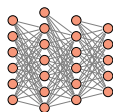
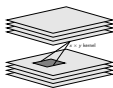


Observations \longrightarrow State Estimation \longrightarrow Modeling & Prediction \longrightarrow Planning \longrightarrow Controls

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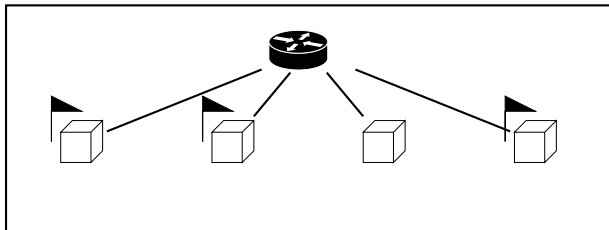
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First Task: v_1

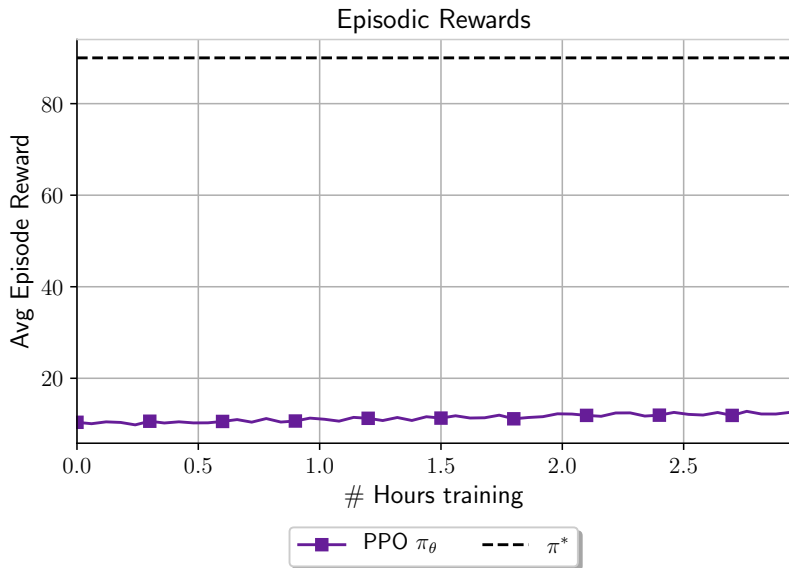


- ▶ **Goal:** Given no prior knowledge, except the IP of the subnetwork $172.18.1.0/24$, learn π_θ^* .

$$\pi_\theta^* = \arg \max_{\pi_\theta \in \Pi_\theta} \mathbb{E} \left[\sum_{t=0}^{\infty} \gamma^t r_{t+1} \right] \quad \Pi_\theta = \{ \pi_\theta \mid \theta \in \mathbb{R}^d \}$$

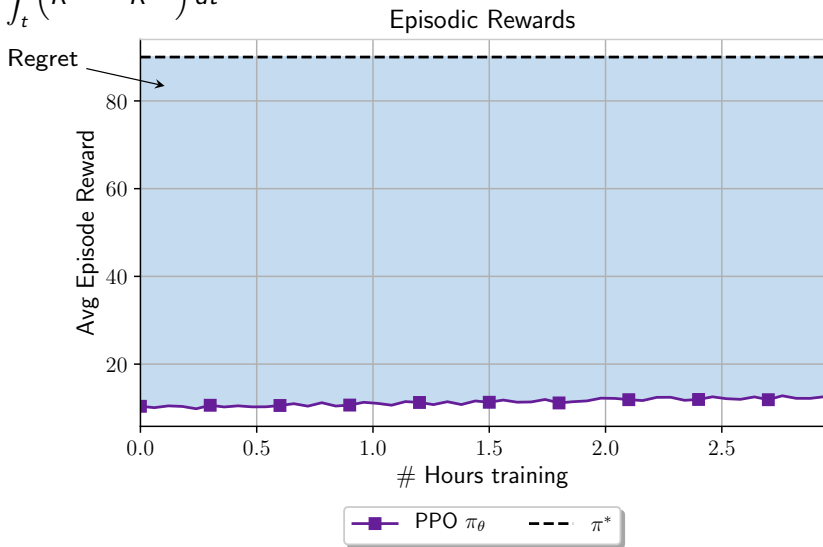
- ▶ π_θ^* : Finds all flags in the minimum number of steps

A First Attempt of the v_1 Task!



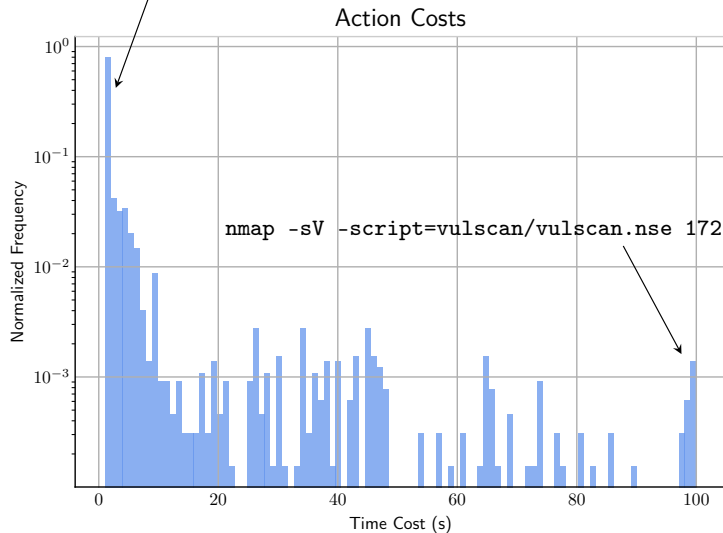
A First Attempt of the v_1 Task!

$$\int_t (R^{\pi^*} - R^{\pi_\theta}) dt$$



Empirical Distribution of Action Costs

```
lftp ftp://u:pw@172.8.3.3
```



Some Assumptions

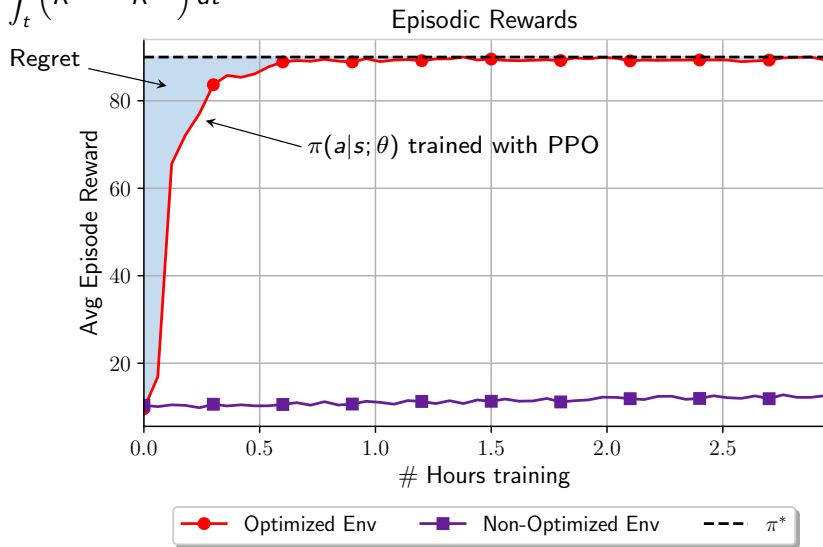
- ▶ With some loss of generality (**but not much**), we can assume a *Partially Synchronous System*
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 - ▶ (strong completeness and eventual strong accuracy)
 - ▶ **Eventual upper bounds** on communication delays
 - ▶ **Crash-stop failure model** extended with omission faults
- ▶ This system model enables optimizations:
 - ▶ **Upper bound** timeout on scanning operations
 - ▶ Scan results can be **cached** for some duration Δ
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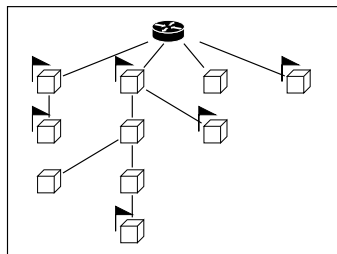
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A Second Attempt of the v_1 Task

$$\int_t (R^{\pi^*} - R^{\pi_\theta}) dt$$



Second Task: v_2



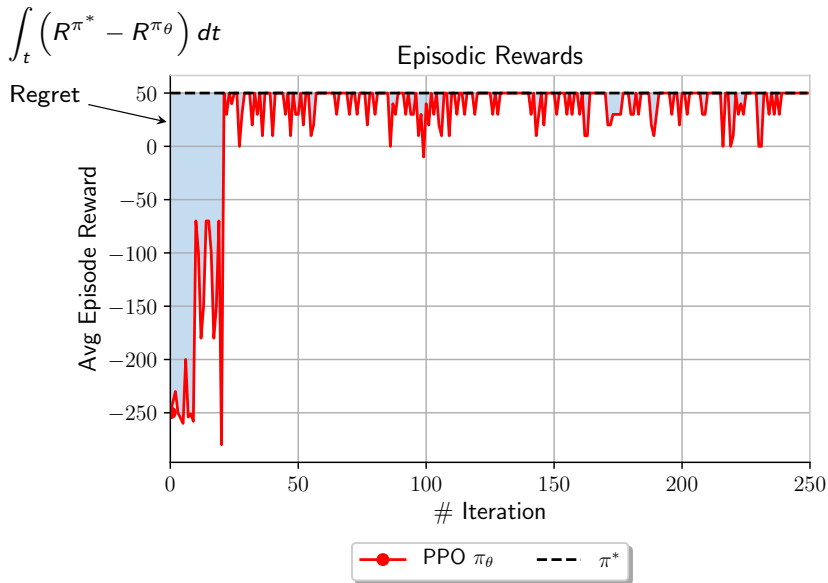
Learning task v_2

- ▶ **Goal:** Given no prior knowledge, except the IP of the subnetwork $172.18.1.0/24$, learn π_θ^* .

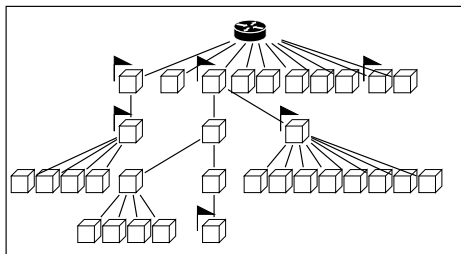
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- ▶ π_θ^* : Finds all flags in the minimum number of steps

v_2 Task Training Results



Third Task: v_3



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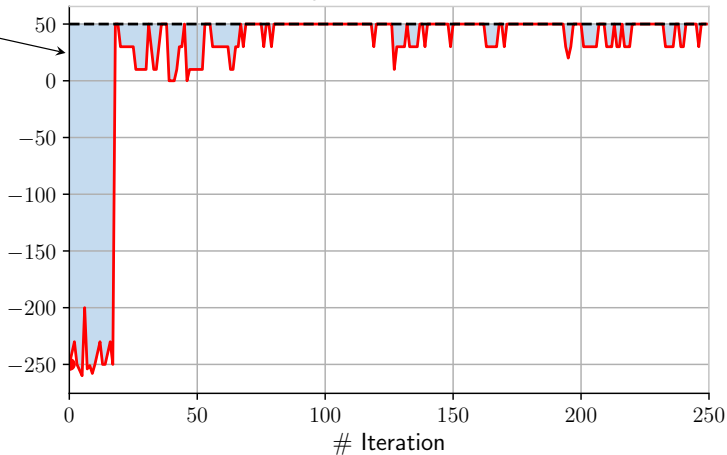
v_3 Task Training Results

$$\int_t (R^{\pi^*} - R^{\pi_\theta}) dt$$

Regret

Episodic Rewards

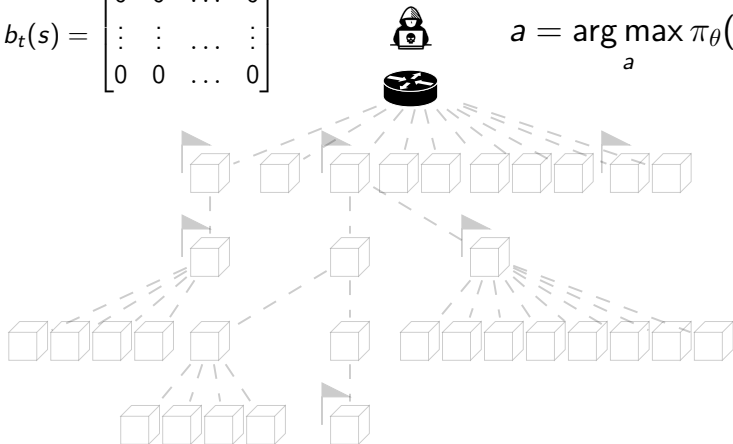
Avg Episode Reward



Example of a Learned Policy π_θ

$$b_t(s) = \begin{bmatrix} 0 & 0 & \dots & 0 \\ \vdots & \vdots & \dots & \vdots \\ 0 & 0 & \dots & 0 \end{bmatrix}$$

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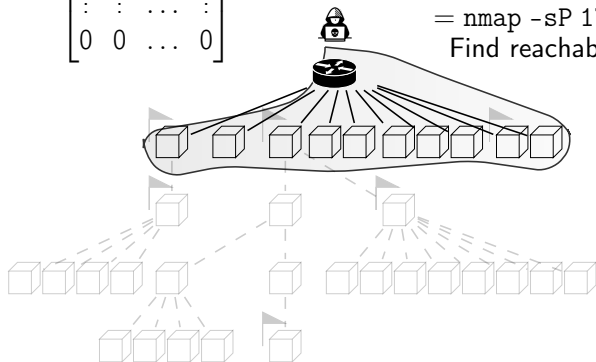
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Find reachable machines on network

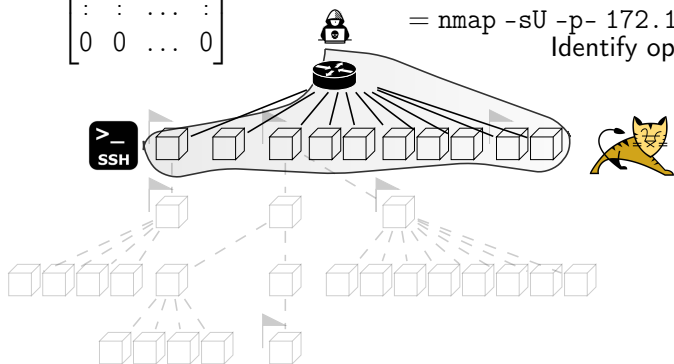


Example of a Learned Policy π_θ

$$b_t = \begin{bmatrix} 1 & 1 & \dots & 0 \\ 1 & 2 & \dots & 0 \\ \vdots & \vdots & \dots & \vdots \\ 0 & 0 & \dots & 0 \end{bmatrix}$$

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= nmap -sU -p- 172.18.3.0/24
Identify open ports



Example of a Learned Policy π_θ

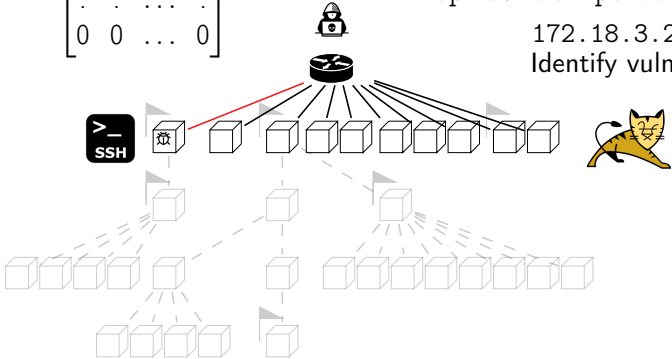
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= nmap -sV -script=vulscan/vulscan.nse

172.18.3.2

Identify vulnerabilities



Example of a Learned Policy π_θ

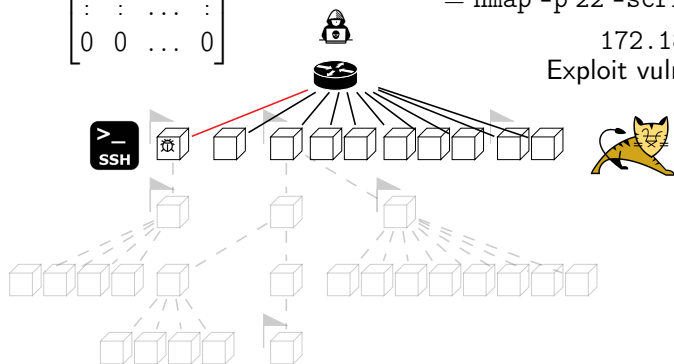
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= nmap -p 22 -script ssh-brute

172.18.3.2

Exploit vulnerability



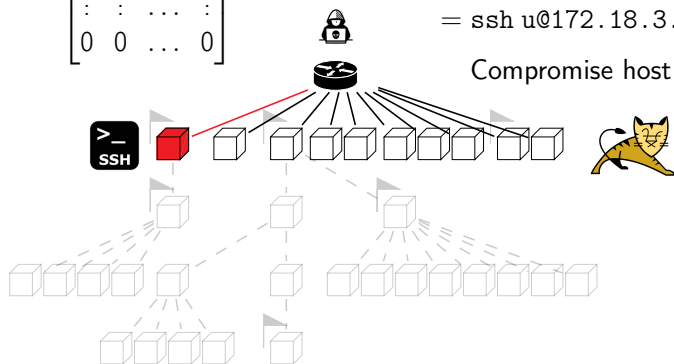
Example of a Learned Policy π_θ

$$b_t = \begin{bmatrix} 1 & 1 & \dots & \mathbf{1} \\ 1 & 2 & \dots & 0 \\ \vdots & \vdots & \dots & \vdots \\ 0 & 0 & \dots & 0 \end{bmatrix}$$

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$$= \text{ssh u@172.18.3.2}$$

Compromise host

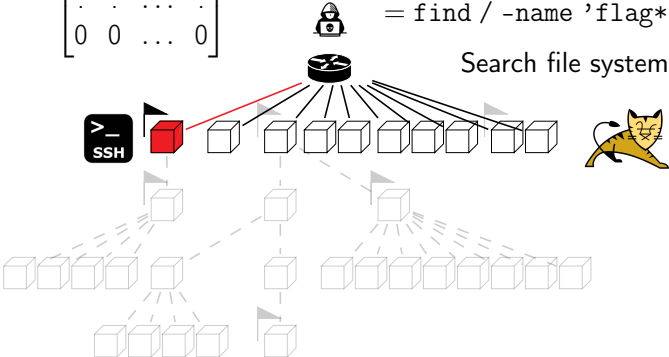


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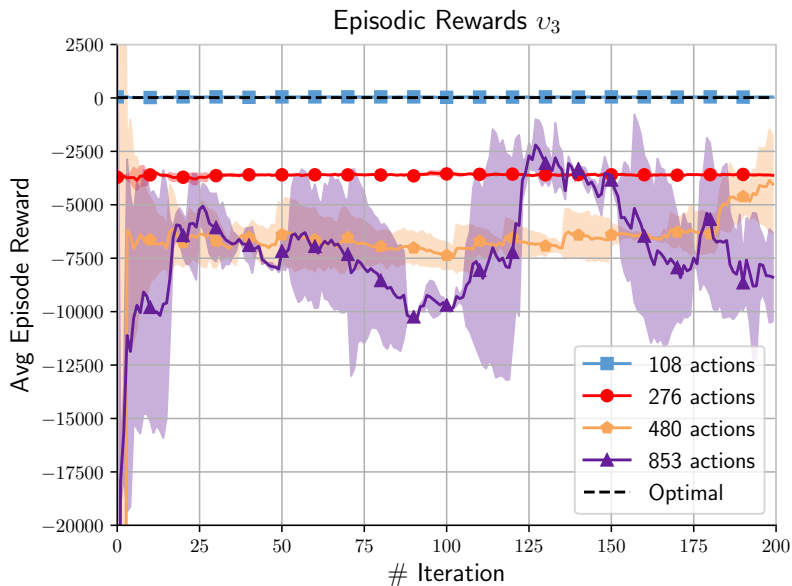
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= find / -name 'flag*.txt'



Challenge: Learning with Large Action Spaces



Action Space Scaling

- ▶ Actions **scale linearly** with the number of nodes $|\mathcal{N}|$.

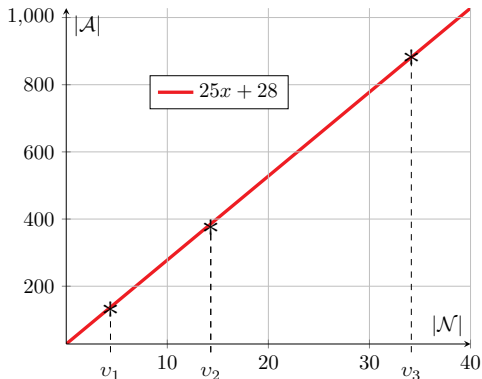
- ▶ $|\mathcal{A}| = \underbrace{25|\mathcal{N}|}_{\text{Node-actions}} + \underbrace{28}_{\text{Subnet actions}}$

- ▶ Large action spaces is a **known challenge** for RL

- ▶ **Reason:** Inflates the policy space Π exponentially

- ▶ Assume Markovian Deterministic Stationary policies

- ▶ $|\Pi| = \frac{(|\mathcal{S}|^{|\mathcal{A}|})^{T-1}}{(|\mathcal{S}|^{|\mathcal{A}|})^{T-1}} =$



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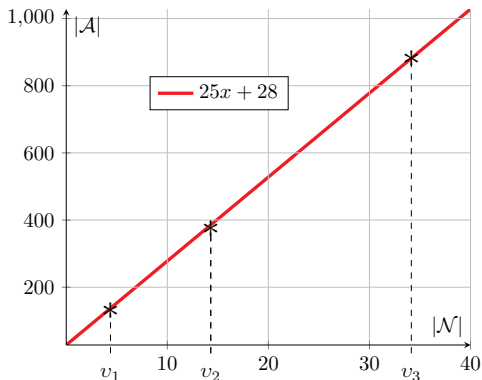
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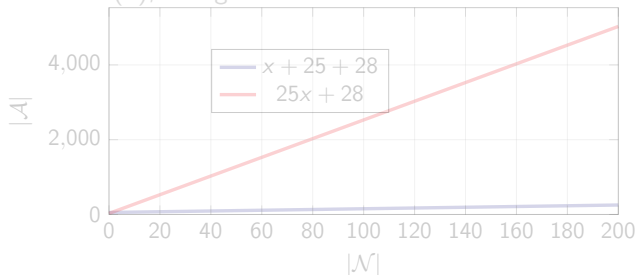


A Possible Solution: Auto-Regressive Policy

- ▶ **Idea:** Represent action a_t as *sequence of sub-actions* (n, a) :
 1. **Select node** in the topology to target (n)
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- ▶ Then, $\pi(a|o) = \pi(a, n|o)$, which can be decomposed into $\pi(a|n, o)$ & $\pi(n|o)$:

$$\pi(a, n|o) = \pi(a|n, o) \cdot \pi(n|o) \quad \text{Chain rule}$$

- ▶ **Reduces the size of the action space** from $25|\mathcal{N}| + 28$ to $|\mathcal{N}| + 25 + 28$
 - ▶ Still $\mathcal{O}(n)$, though.

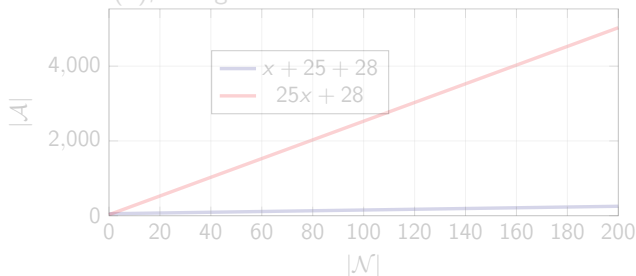


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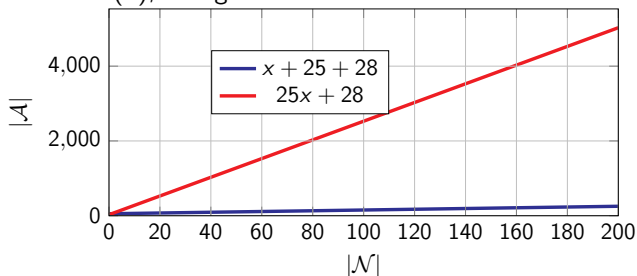


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- ▶ We investigate how to combine real security applications with decision theory/learning theory methods.
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